

# BA01 - Mathematics for Technicians FORMULAS

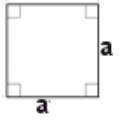
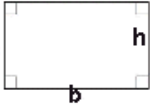
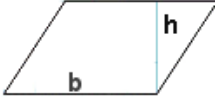
$$a^2 = a \times a$$

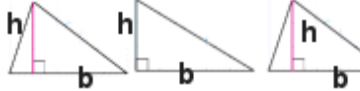
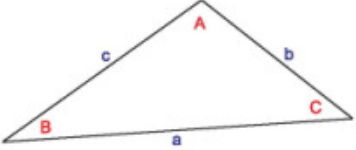
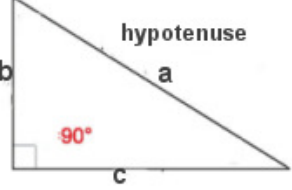
$$\sqrt{a^2} = a$$

$$1\% = 0.01 = 1/100$$

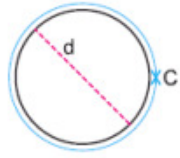
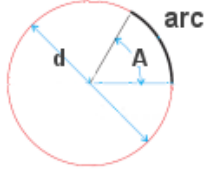
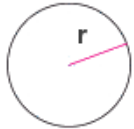
$$\frac{a}{b} = \frac{c}{d} \Leftrightarrow a \times d = b \times c$$

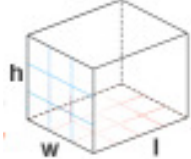
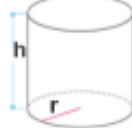

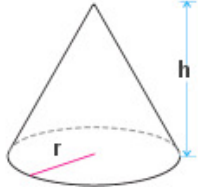
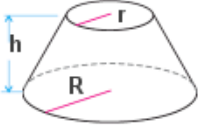
## GEOMETRY

|                         |              |  |
|-------------------------|--------------|--|
| Area of a Square        | $a \times a$ |   |
| Area of a Rectangle     | $b \times h$ |  |
| Area of a Parallelogram | $b \times h$ |  |

|                      |                         |  |
|----------------------|-------------------------|--|
| Area of a Triangle   | $\frac{b \times h}{2}$  |  |
| Angles of a Triangle | $A + B + C = 180^\circ$ |  |
| Pythagorean Theorem  | $a^2 = b^2 + c^2$       |  |

|  |
|--|
| $\text{Pi} = \pi \approx 3.1416. \approx 3.14$ |
|--|

|                           |                                     |   |
|---------------------------|-------------------------------------|---|
| Circumference of a Circle | $2 \pi r$                           |  |
| Arc Length                | $\frac{\pi \times d \times A}{360}$ |  |
| Area of a Circle          | $\pi r^2$<br>or $\frac{\pi d^2}{4}$ |  |

|                                       |  |   |
|---------------------------------------|--|---|
| Volume of a Cube                      | $w \times l \times h$                                      |  |
| Volume of a Cylinder                  | $\pi r^2 h$  |  |
| Volume of a Sphere                    | $\frac{4 \pi r^3}{3}$                                      |  |
| Volume of a Cone                      | $\frac{\pi r^2 \times h}{3}$                               |  |
| Volume of a Conical Section (Frustum) | $\frac{\pi \times h \times (R^2 + [R \times r] + r^2)}{3}$ |  |

## TRIGONOMETRY

|  |   |  |
|--|---|--|
| $\text{Sin} = \frac{\text{opposite side}}{\text{hypotenuse}}$    | $\text{Sin } B = \frac{b}{a} \quad \text{Sin } C = \frac{c}{a}$ |  |
| $\text{Cos} = \frac{\text{adjacent side}}{\text{hypotenuse}}$    | $\text{Cos } B = \frac{c}{a} \quad \text{Cos } C = \frac{b}{a}$ |  |
| $\text{Tan} = \frac{\text{opposite side}}{\text{adjacent side}}$ | $\text{Tan } B = \frac{b}{c} \quad \text{Tan } C = \frac{c}{b}$ |  |

## PREFIXES IN THE METRIC SYSTEM

| Prefix | Factor    | Example    | Description                      |
|--------|-----------|------------|----------------------------------|
| giga   | $10^9$    | gigahertz  | one billion hertz                |
| mega   | $10^6$    | megaton    | one million tons                 |
| kilo   | $10^3$    | kilometer  | one thousand meters              |
| hecto  | $10^2$    | hectometer | one hundred meters               |
| deka   | $10^1$    | dekaliter  | ten liters                       |
| deci   | $10^{-1}$ | decigram   | one <i>tenth</i> of a gram       |
| centi  | $10^{-2}$ | centimeter | one <i>hundredth</i> of a meter  |
| milli  | $10^{-3}$ | milliliter | one <i>thousandth</i> of a liter |
| micro  | $10^{-6}$ | microgram  | one <i>millionth</i> of a gram   |
| nano   | $10^{-9}$ | nanosecond | one <i>billionth</i> of a second |

## CONVERSION FACTORS

### DISTANCE, WEIGHT AND VOLUME CONVERSION FACTORS

| Multiply    | By     | To get      |
|-------------|--------|-------------|
| inches      | 2.54   | centimeters |
| centimeters | .3937  | inches      |
| feet        | .3048  | meters      |
| meters      | 3.2808 | feet        |
| yards       | .9144  | meters      |
| meters      | 1.0936 | yards       |
| miles       | 1.6094 | kilometers  |
| kilometers  | .6214  | miles       |
| pounds      | .4536  | kilograms   |
| kilograms   | 2.2046 | pounds      |
| quarts      | .9463  | liters      |
| liters      | 1.0568 | quarts      |

### TEMPERATURE CONVERSIONS

$$\text{deg F} = \frac{9 \times \text{deg C}}{5} + 32$$

$$\text{deg C} = \frac{5 \times (\text{deg F} - 32)}{9}$$

$$\text{deg K} = \text{deg C} + 273.2$$

### PRESSURE CONVERSIONS

$$\text{Pressure (Pa)} = \text{Pressure (psi)} \times 6,895$$

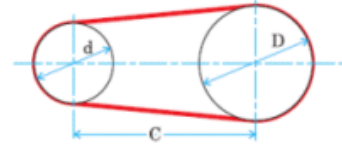
$$\text{Pressure (psi)} = \text{Pressure (kiloPa)} \times 0.14503$$

$$\text{Pressure (bars)} = \frac{\text{Pressure (kiloPa)}}{100}$$

## MECHANICS

### BELT LENGTH

$$\text{Length} = L = (2 \times C) + 1.57 \times (D + d) + \frac{(D - d)^2}{4 \times C}$$



### CHAIN LENGTH IN NUMBER OF LINKS

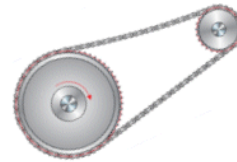
$$L = \frac{N + n}{2} + \frac{2C}{P} + \left( \frac{N - n}{2\pi} \right)^2 \left( \frac{P}{C} \right)$$

**P** = the pitch of the chain (inches or mm per link)

**C** = the distance between the centers of the drive and driven sprockets (in inches or mm)

**N** = number of teeth on the large sprocket

**n** = number of teeth on the small sprocket



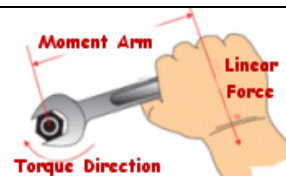
### SHAFT SPEED

$$\text{Driven Speed} = \frac{\text{Drive Diameter} \times \text{Drive Speed (RPM)}}{\text{Driven Diameter}}$$

$$\text{Drive Speed} = \frac{\text{Driven Diameter} \times \text{Driven Speed (RPM)}}{\text{Drive Diameter}}$$

### TORQUE

$$\text{Torque} = \text{Moment Arm} \times \text{Linear Force}$$



## SPEED AND ANGULAR VELOCITY

|   |
|---|
| distance = speed x time   |
| $\text{Angular Velocity} = \frac{\text{Angle (in degrees, revolutions or radians)}}{\text{Time (in seconds or minutes)}}$ |
| $1 \text{ revolution} = 360 \text{ degrees}$ $= 2\pi \text{ radians}$   |
| Number of revolutions = rpm x time (min)  |
| $\text{Linear speed (ft or m/s)} = \frac{\text{rpm} \times 2 \pi r \text{ (ft or m)}}{60 \text{ (s/min)}}$                |

## DISTANCE, SPEED AND ACCELERATION

|   |
|---|
| $\text{speed}_{\text{final}} = \text{speed}_{\text{initial}} + \text{acceleration} \times t$ $t = \frac{\text{speed}_{\text{final}} - \text{speed}_{\text{initial}}}{\text{acceleration}}$ $\text{distance} = \text{speed}_{\text{average}} \times t$ $\text{speed}_{\text{average}} = \frac{1}{2} (\text{speed}_{\text{final}} + \text{speed}_{\text{initial}})$ $\text{distance} = \frac{1}{2} \frac{(\text{speed}_{\text{final}} - \text{speed}_{\text{initial}})^2}{\text{acceleration}}$ $\text{acceleration} = \frac{1}{2} \frac{(\text{speed}_{\text{final}} - \text{speed}_{\text{initial}})^2}{\text{distance}}$ |
|---|

|                      |                           |
|----------------------|---------------------------|
| Gravity acceleration | G = 32 ft/sec = 9.8 m/sec |
|----------------------|---------------------------|

## FORCE, WORK/ENERGY AND POWER

|                             |
|-----------------------------|
| Force = Mass x Acceleration |
| Work = Force x Distance     |

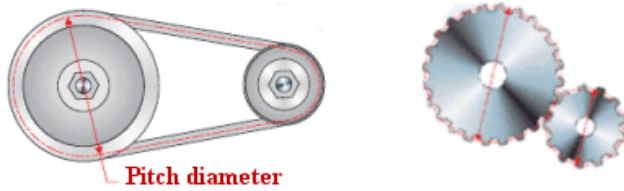
|   |
|---|
| Energy = Work   |
| Kinetic Energy = $\frac{1}{2}$ Mass x Velocity <sup>2</sup> |
| Power = Work /Time  |

### DRIVE RATIOS

$$\text{output speed} = \frac{\text{input speed X input pitch diameter}}{\text{output pitch diameter}}$$

$$\text{output torque} = \frac{\text{input torque X output pitch diameter}}{\text{input pitch diameter}}$$

$$\text{output speed X output torque} = \text{input speed X input torque}$$



### OHM'S LAW

|                  |   |
|------------------|---|
| $E = I \times R$ | E is Electric potential (Volts)<br>I is Current (Amperes)<br>R is Resistance (Ohms) |
|------------------|---|

**HYDRAULICS**

|                  |  |
|------------------|--|
| $F = P \times A$ | F is total force due to pressure<br>P is pressure<br>A is area |
|------------------|--|

|   |
|---|
| $\text{Pressure (Pa)} = \text{Pressure (psi)} \times 6,895$       |
| $\text{Pressure (psi)} = \text{Pressure (kiloPa)} \times 0.14503$ |
| $\text{Pressure (bars)} = \frac{\text{Pressure (kiloPa)}}{100}$   |

|  |
|--|
| $\text{Head} = \frac{\text{Fluid density}}{\text{water density}} \times \text{Fluid height}$ |
|--|